



linear in parameters:

$$\sum w_i \cdot \square$$

can't involve any w_s !

function of \vec{x} only

Question 🤔 (Answer at practicaldsc.org/q)

Which hypothesis function is **not** linear in the parameters?

✓ A. $H(\vec{x}) = w_1(x^{(1)}x^{(2)}) + \frac{w_2}{x^{(1)}} \sin(x^{(2)})$

• B. $H(\vec{x}) = 2^{w_1} x^{(1)}$ w_1 is being exponentiated! non-linear \vec{x} only

✓ C. $H(\vec{x}) = \vec{w} \cdot \text{Aug}(\vec{x})$

• D. $H(\vec{x}) = w_1 \cos(x^{(1)}) + w_2 2^{x^{(2)} \log x^{(3)}}$

• E. More than one of the above.

$\vec{w} \cdot \text{Aug}(\vec{x}) = w_0 + w_1 x^{(1)} + w_2 x^{(2)} + \dots$

as linear as it gets!

$\text{Aug}(\vec{x}) =$

$$\begin{bmatrix} 1 \\ x^{(1)} \\ x^{(2)} \\ \vdots \\ x^{(d)} \end{bmatrix}$$

?



$H(x) = \omega_0 e^{\omega_1 x}$ not currently linear!

Idea: take log of both sides

$$\log H(x) = \log(\omega_0 e^{\omega_1 x})$$

$$\log H(x) = \underbrace{\log(\omega_0)}_{b_0} + \underbrace{\omega_1 x}_{b_1}$$

use the relationships:

$$\omega_1^* = b_1^*$$

$$\omega_0^* = e^{b_0^*}$$

find the b_i^* from normal eqns

$\Rightarrow T(x) = b_0 + b_1 x \Rightarrow$ is linear in its parameters!!!

$$X = \begin{bmatrix} 1 & x_1 \\ \vdots & \vdots \\ 1 & x_n \end{bmatrix}_{n \times 2}$$

$$\vec{b} = \begin{bmatrix} b_0 \\ b_1 \end{bmatrix}$$

solve normal equations for b_0^*, b_1^*

$$\vec{t} = \begin{bmatrix} \log y_1 \\ \log y_2 \\ \vdots \\ \log y_n \end{bmatrix}$$



- Suppose we have the following fitted model:

For illustration, assume 'weekend' was originally a categorical feature with two possible values, 'Yes' or 'No'.

$$H(x) = 1 + 2 \cdot (\text{weekend}==\text{Yes}) - 2 \cdot (\text{weekend}==\text{No})$$

- This is equivalent to:

$$H(x) = 10 - 7 \cdot (\text{weekend}==\text{Yes}) - 11 \cdot (\text{weekend}==\text{No})$$

- Note that for a particular row in the dataset, weekend==Yes + weekend==No is always equal to 1.

$$X = \begin{bmatrix} | & | & | \\ | & 0 & 0 \\ | & \vdots & \vdots \\ | & | & | \\ | & 0 & 0 \\ | & \vdots & \vdots \\ | & | & | \end{bmatrix}$$

①
Yes ②
No ③

col ② + col ③ = col ①
 \Rightarrow X's columns are not linearly independent!
 \Rightarrow X is not full rank
 \Rightarrow $X^T X$ is not invertible!
 \Rightarrow infinitely many solutions to $X^T X \vec{w} = X^T \vec{y}$

?

$$X^T X \vec{w} = X^T \vec{y}$$

```
In [65]: stdscaler.var_
```

```
Out[65]: array([ 3.89, 35191.58, 13.72, 25.44, 23.08])
```

- If needed, the `fit_transform` method will fit the transformer and then transform the data in one go.

```
In [66]: new_scaler = StandardScaler()
```

```
In [68]: stdscaler.transform(sales.iloc[:, 1:].tail(5))
```

```
Out[68]: array([[ -1.13, -1.31, -1.35, -1.6 ,  0.89],  
               [  0.14,  0.39,  0.4 ,  0.32, -0.36],  
               [  0.09, -0.03,  0.46,  0.36, -0.57],  
               [  0.9 ,  1.08,  1.05,  1.19, -1.61],  
               [ 2.67,  0.69, -0.3 ,  0.46,  0.05]])
```

fit on all rows.

Why are these values different?

```
In [69]: new_scaler.fit_transform(sales.iloc[:, 1:].tail(5))
```

```
Out[69]: array([[ -1.33, -1.79, -1.71, -1.88,  1.48],  
               [-0.32,  0.28,  0.43,  0.19, -0.05],  
               [-0.36, -0.24,  0.49,  0.23, -0.31],  
               [ 0.29,  1.11,  1.22,  1.13, -1.58],  
               [ 1.71,  0.64, -0.43,  0.34,  0.46]])
```

fit on last 5 rows?

?